

# Component Separation: Large-Aperture Frequency Channel Distribution (T + P)

Colin Hill

Institute for Advanced Study  
Flatiron Institute - Center for Computational Astrophysics

CMB-S4 Meeting, Harvard  
25 August 2017



# Sky Model: Temperature

**Model constructed from full-sky numerical sims. + data**

Components:

$N_{\text{side}}=4096$

- Lensed CMB (via ray-traced N-body simulation)
- Thermal Sunyaev-Zel'dovich
- Kinematic Sunyaev-Zel'dovich
- Cosmic infrared background (CIB)
- Radio point sources (flux cut = 7 mJy at 150 GHz)
- Galactic dust
- Galactic synchrotron (Planck Commander template)
- Galactic free-free (Planck Commander template)
- Galactic anomalous microwave emission (Planck Commander)
- Atmosphere ( $l_{\text{knee}}=3400$ ,  $\alpha_{\text{knee}} = -4.7$ ) [frequency-independent]

tSZ and CIB rescaled  
to match recent data

caveat: no power  
in Commander  
above  $ell \sim 400$

All components are properly correlated

# Sky Model: Polarization

## Analytic model based on BICEP2 foreground analysis

### Components:

- Galactic dust (modified blackbody SED and  $\sim \ell^{-2.4}$ )
- Galactic synch (power-law SED in antenna temp and  $\sim \ell^{-2.3}$ )
  - Includes a dust-correlated component ( $r_{\text{dust-synch}}=0.7$ )
- Polarized radio point sources (power-law SED in flux units)
- Lensed CMB ( $r=0$ )
- Atmosphere ( $l_{\text{knee}}=330$ ,  $\alpha_{\text{knee}} = -3.8$ ) [frequency-independent]

### Assumptions:

- Dust and synch. amplitudes match BICEP2 region for  $f_{\text{sky}}=0.01$
- Dust and synch. amplitudes scale as  $\sqrt{f_{\text{sky}}}$  for larger  $f_{\text{sky}}$
- (Dust or synch EE amplitude)/(Dust or synch BB amplitude) = 2

# Internal Linear Combination (ILC)

relatively agnostic approach, flexible choice of domain

$$\Delta T_i(p) = a_i y(p) + n_i(p) \quad i \longleftrightarrow \text{frequency}$$

observed temperature  
fluctuation

component  
of interest

noise+  
contaminants

minimum variance estimator with unit response to desired component:

$$\hat{y}(p) = w_i \Delta T_i(p) \quad w_j = \frac{a_i (\hat{R}^{-1})_{ij}}{a_k (\hat{R}^{-1})_{kl} a_l}$$

$$\hat{R}_{ij} = N_{\text{pix}}^{-1} \sum_p \Delta T_i(p) \Delta T_j(p)$$

flexibility = choice of domain on which to compute covariance

# Constrained ILC

extension: explicitly remove other component(s) as well

$$\Delta T_i(p) = a_i y(p) + b_i s(p) + n_i(p)$$

observed temperature  
fluctuation

component  
of interest

component  
to remove

noise + other  
contaminants

minimum variance estimator with unit response to desired component  
and zero response to undesired component:

$$w_j = \frac{\left( b_k (\hat{R}^{-1})_{kl} b_l \right) a_i (\hat{R}^{-1})_{ij} - \left( a_k (\hat{R}^{-1})_{kl} b_l \right) b_i (\hat{R}^{-1})_{ij}}{\left( a_k (\hat{R}^{-1})_{kl} a_l \right) \left( b_m (\hat{R}^{-1})_{mn} b_n \right) - \left( a_k (\hat{R}^{-1})_{kl} b_l \right)^2}$$

- can be extended to explicitly remove N components
- advantage: can remove contaminants that could bias some analysis
- disadvantage: variance in final ILC map is larger

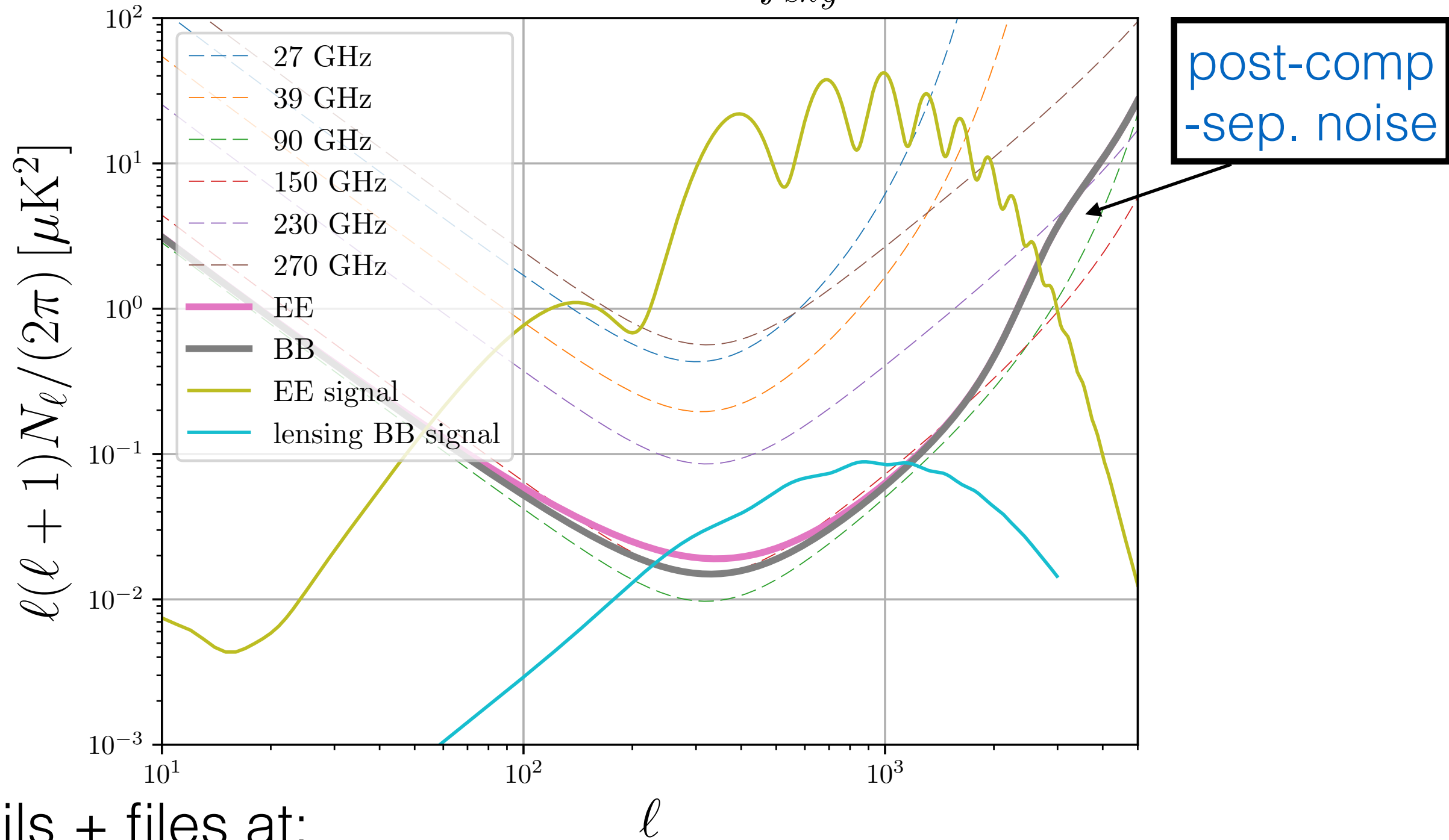
# Pipeline Summary

1. Compute signal auto- and cross-power spectra [TT/EE/BB] at all frequencies for all  $f_{\text{sky}}$  options
2. Compute map noise power spectra for all channel configuration options **SO Calculator** *can be re-done for any desired channel config.*
3. Run harmonic-space [constrained] ILC to obtain post-component-separation noise for CMB, kSZ, and tSZ signals
4. Evaluate signal-to-noise of desired observables:
  1. Total Blackbody Power Spectrum [CMB+kSZ+ISW] ( $l_{\text{max}} = 10000$ )
  2. Kinematic SZ Power Spectrum ( $3000 < l < 10000$ )
  3. Thermal SZ Power Spectrum (proxy for tSZ cluster probes) ( $l_{\text{max}} = 10000$ )
  4. CMB Lensing Power Spectrum via TT Estimator ( $l_{\text{max}} = 3000$ )
  5. CMB Lensing Power Spectrum via EB Estimator ( $l_{\text{max}} = 5000$ )
  6. Lensing BB Power Spectrum ( $l_{\text{max}} = 5000$ )

# Example: Pol. Noise Curves

explicit deprojection of [fiducial] dust and synchrotron components  
optimization for EB lensing S/N

500000 detectors +  $f_{sky} = 0.4$



Details + files at:

[https://cmb-s4.org/CMB-S4workshops/index.php/R-forecasting:high\\_and\\_low\\_ell\\_coordination](https://cmb-s4.org/CMB-S4workshops/index.php/R-forecasting:high_and_low_ell_coordination)